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- Bigger picture: how can *multiple* people – with differing values – divide an infinitely divisible resource in such a way that everyone prefers the share they ultimately end up with (i.e., is envy-free)?

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Don't forget to bring cake!

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- That is why I love it!